

$$1) (y^5 - y^2 + 6y - 4) : (y+1)$$

	1	0	0	-1	6	-4
-1		-1	1	-1	+2	-8
	<u>1</u>	<u>-1</u>	<u>1</u>	<u>-2</u>	<u>8</u>	-12

$$Q(y) = y^4 - y^3 + y^2 - 2y + 8$$

$$R(y) = -12$$

$$\begin{aligned}
 2) \frac{1}{2}b^3 + b^2 + 2bc + 4c^2 + 2bc^2 + 4bc &= \\
 &= (b+2c)^2 + \frac{1}{2}b(b^2 + 4bc + 4c^2) = \\
 &= (b+2c)^2 + \frac{1}{2}b(b+2c)^2 = \\
 &= (b+2c)^2 \left(1 + \frac{1}{2}b\right)
 \end{aligned}$$

$$3) \quad a^3 - 5a^2 + 3a + 9 \quad \begin{array}{l} \pm 1 \\ \pm 3 \\ \pm 9 \end{array}$$

$$R(1) = 1 - 5 + 3 + 9 \neq 0$$

$$R(-1) = (-1)^3 - 5(-1)^2 + 3(-1) + 9 = \\ = -1 - 5 - 3 + 9 = 0$$

$$\begin{array}{c|ccc|c} & 1 & -5 & 3 & 9 \\ \textcircled{-1} & & -1 & 6 & -9 \\ \hline & \underline{1} & \underline{-6} & \underline{9} & // \end{array}$$

$$a^3 - 5a^2 + 3a + 9 = (a+1)(a^2 - 6a + 9) = \\ = (a+1)(a-3)^2$$

$$4) 6x^2 + 5x + 1$$

$$R(1) = 6 + 5 + 1 = 12 \neq 0$$

$$R(-1) = 6 - 5 + 1 = 2 \neq 0$$

$$R\left(\frac{1}{2}\right) = 6 \cdot \frac{1}{4} + 5 \cdot \frac{1}{2} + 1 \neq 0$$

$$R\left(-\frac{1}{2}\right) = \cancel{6} \cdot \frac{1}{4} - 5 \cdot \frac{1}{2} + 1 = 0$$

$\pm 1$	$\pm 1$
$\pm 2$	
$\pm 3$	
$\pm 6$	
	$\pm \frac{1}{2}$
	$\pm \frac{1}{3}$
	$\pm \frac{1}{6}$

$-\frac{1}{2}$	6	5	1
	6	-3	-1
	6	2	0

$$\left(x + \frac{1}{2}\right) (6x + 2)$$

Teorema:  $a_2x^2 + a_1x + a_0 = 0$

$\frac{p}{q} \in \mathbb{Q}$  con  $p|a_0$  e  $q|a_2$

$$b|a \Leftrightarrow a = br$$